
Correction

Exercice 1. Evaluer la suite d'expressions suivante :

let x=0;;	# val x : int = 0
x=0;;	# - : bool = true
x;;	# - : int = 0
0;;	# - : int = 0
2+2;;	# - : int = 4
x=1;;	# - : bool = false
if x=1 then 0 else 1;;	# - : int = 1
let x=1 and y=2;;	# val x : int = 1 val y : int = 2
let x=y;;	# val x : int = 2
x=y;;	# - : bool = true
let z=1 and y=z;;	# Unbound value z
let x=y+1;;	# val x : int = 3
let x=4 in y=4;;	# - : bool = false
x;;y;;	# - : int = 3 (- : int = 2 non évaluée)
let y=let x=0 in 4;;	# val y : int = 4
let y=let x=0 and y=4;;	# Syntax error
let y=if x=0 then 4 else 5;;	# val y : int = 5
let y= let x=1 in if x=0 then 4 else 5;;	# val y : int = 5
x;;	# - : int = 3
y;;	# - : int = 5
let x=2 and y=x+2;;	# val x : int = 2 val y : int = 5
let x=1 in y=x+2;;	# - : bool = false
x;;	# - : int = 2
let y= let x=1 in x+2;;	# val y : int = 3
let x=x+1 and let y=x+4;;	# Syntax error
x;; y;;	# - : int = 2 (- : int = 3 non évaluée)
let x=2 in let y=2;;	# Syntax error
let x=2 in let y=2 in x*x+y;;	# - : int = 6
let x=3 and y=2 in x*x+y;;	# - : int = 11
let x=2 in let y=x+1 in x*x+y;;	# - : int = 7
let x=4 and y=x+1 in x*x+y;;	# - : int = 19
let x=2;;	# val x : int = 2
let x=x*x;;	# val x : int = 4
let x= let x=3 in x*x;;	# val x : int = 9
let x=1;;	# val x : int = 1
let x=2 in x*4;;	# - : int = 8
x;;	# - : int = 1
let x = 5 in let x = 2 and y = x*x in 2*y*x;;	# - : int = 100
let x=1 in let x=x+1 in x+3;;	# - : int = 5
let x=1 in let x=x+1 and y=x+2 in x+y;;	# - : int = 5
let x=1 and y=2 and z=3 in y*y-4*x*z;;	# - : int = -8
let x=1 and x=2 and x=3 in y*y-4*x*z;;	# This variable is bound several times in this matching

Exercice 2. Même question que précédemment ...

```

let f=function x -> 1;;
let f=function x -> x;;
f;;
let f=function x -> x+1;;
let f x= x+1;;
let f(x)=x+1;;
(f 1);;
f 1;;
f(1);;
(f(f 1));;
(f f 1);;
let f=function x -> function y -> x+y;;
(f 1);;
((f 1) 2);;
(f 1 2);;
f (1,2);;

f(1 2);;

let f=function x -> (f x);;
(f 1);;
(f 1 2);;
let g=function x -> (f x);;
(g 1);;
(g 1 2);;
let h=function x -> (h x);;
let x=3 in ((function x -> x+x) 4);;
let x=3 in ((function y -> y+y) x);;
let x=3 in ((function y -> x+y) 4);;
let y=4 in let x=3 in ((function y -> x+y) y);;
let y=4 in let x=3 in ((function y -> x+y) x);;
let f= function (x-> let y=2 in x+y);;

let f= function x-> let y=2 in x+y;;
let f= function x-> let y=2 and let x=x+y;;
let x=7 in let f(y)=y*x
  in let x=true in if x then (f 3) else (f 2);;
let x=1+2 in ((function y->y+x) x);;
let x=1+2 in ((function x->x+x) x);;
let x = 5 in let x = 4
  in let f = function x -> x*x in f x;;

```

```

# val f : 'a -> int = <fun>
# val f : 'a -> 'a = <fun>
# - : 'a -> 'a = <fun>
# val f : int -> int = <fun>
# val f : int -> int = <fun>
# val f : int -> int = <fun>
# - : int = 2
# - : int = 2
# - : int = 2
# - : int = 3
# This function is applied to too many arguments
# val f : int -> int -> int = <fun>
# - : int -> int = <fun>
# - : int = 3
# - : int = 3
# This expression has type int * int but
is here used with type int
# This expression is not a function,
it cannot be applied
# val f : int -> int -> int = <fun>
# - : int -> int = <fun>
# - : int = 3
# val g : int -> int -> int = <fun>
# - : int -> int = <fun>
# - : int = 3
# Unbound value h
# - : int = 8
# - : int = 6
# - : int = 7
# - : int = 7
# - : int = 6
# Syntax error: ')' expected, the highlighted
'(' might be unmatched
# val f : int -> int = <fun>
# Syntax error
# - : int = 21
# - : int = 6
# - : int = 6
# - : int = 16

```

Exercice 3. Soient f et g deux fonctions respectivement déclarées par

```
let f = function x -> x ;; et let g= function h -> function x -> (h x) ;;
```

Quel est leur type ?

```
# val f : 'a -> 'a = <fun> et # val g : ('a -> 'b) -> 'a -> 'b = <fun>
```

Evaluer les expressions suivantes :

```

let h = function x -> x+1 ;;
(f 1) ;;
(f h) ;;
(f h 1) ;;
(g 1) ;;
(g h) ;;
(g h 1) ;;
let g2 = function h ->
  function x -> (h x+1) in (g2 h 1) ;;
let f1 = function f2 -> (function x -> f2 x) in
  let g = function x -> x+1 in f1 g 2 ;;

```

```

# val h : int -> int = <fun>
# - : int = 1
# - : int -> int = <fun>
# - : int = 2
This expression has type int but is here
used with type 'a -> 'b
# - : int -> int = <fun>
# - : int = 2
# - : int = 3
# - : int = 3

```

Exercice 4. Ecrire une fonction *implique* qui pour deux booléens A et B calcule la valeur de vérité de $A \Rightarrow B$.

```
let implique a b = if a then b else true;; (* implique : bool -> bool -> bool = <fun> *)
let implique = function a -> function b -> not a || b;; (* implique : bool -> bool -> bool = <fun>*)
let implique a = function b -> not a || b;; (* implique : bool -> bool -> bool = <fun> *)
```

Évaluer les expressions suivantes :

```
(implique false);;          #- : bool -> bool = <fun>
let f=(implique false) in (f true);;  #- : bool = true
implique (false);;           #- : bool -> bool = <fun>
implique true false;;        #- : bool = false
implique false false;;       #- : bool = true
implique (true false);;      <erreur>
```

Exercice 5. Ecrire une fonction *concat* qui prend trois chaînes de caractères et les concatène.

```
let concat s1 s2 s3 = s1^s2^s3;;
let concat = function s1 -> function s2 -> function s3 -> s1^s2^s3;;
(* #concat : string -> string -> string -> string = <fun> *)
```

Évaluer les expressions suivantes :

```
let f = concat "toto" in          #- : string = "toto est la"
    let g = (f " est ") in (g "la");;
let f=(concat "toto");;           #f : string -> string -> string = <fun>
let f=(f " a ");;                 #f : string -> string = <fun>
let f=(f "faim");;                #f : string = "toto a faim"
(f "?");;                         This expression is not a function, it cannot be applied.
f;;                               #- : string = "toto a faim"
(concat "toto" " plus " "faim");; #- : string = "toto plus faim"
(((concat "ben") " si ") "finalement");; #- : string = "ben si finalement"
```