

# Verification of security protocols *from confidentiality to privacy*

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# Cryptographic protocols everywhere !



**Goal:** they aim at securing communications over public/insecure networks

# Some security properties

- **Secrecy**: May an intruder learn some secret message between two honest participants?
- **Authentication**: Is the agent **Alice** really talking to **Bob**?
- **Anonymity**: Is an attacker able to learn something about the identity of the participants who are communicating?
- **Non-repudiation**: **Alice** sends a message to **Bob**. **Alice** cannot later deny having sent this message. **Bob** cannot deny having received the message.
- ...

# Example: E-voting application



**Eligibility:** only legitimate voters can vote, and only once

**No early results:** no early results can be obtained which could influence the remaining voters

**Vote-privacy/Receipt-freeness/Coercion-resistance:** the fact that a particular voted in a particular way is not revealed to anyone

**Individual/Universal verifiability:**

a voter can verify that her vote was really counted, and that the published outcome is the sum of all the votes



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cryptographic primitives = basic building blocks

→ symmetric/ asymmetric encryption, signature, hash function, ...

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## Symmetric encryption



**Examples:** Caesar cipher, Enigma machine (~ 1918-1945), or more recently DES (1973) and AES (1997)



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## Asymmetric encryption



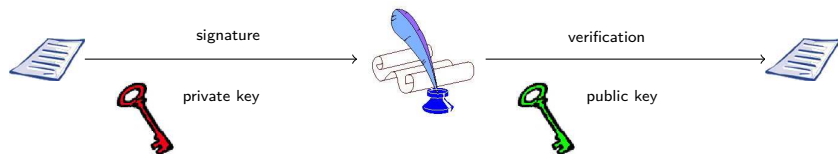
**Examples:** First system published by Diffie-Hellman (1976), RSA (1977)

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## Signature





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**Example:** A simplified version of the Denning-Sacco protocol (1981)

$A \rightarrow B$  :  $\text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B))$

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2.  $C(A) \rightarrow B : \text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B))$

3.  $B \rightarrow A : \text{senc}(s, k)$  **Attack !**

# Exercise

We propose to fix the Denning-Sacco protocol as follows:

## Version 1

$$\begin{aligned} A \rightarrow B & : \text{aenc}(\langle A, B, \text{sign}(k, \text{priv}(A)) \rangle, \text{pub}(B)) \\ B \rightarrow A & : \text{senc}(s, k) \end{aligned}$$

## Version 2

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Which version would you prefer to use?      Version 2

→ Version 1 is still vulnerable to the aforementioned attack.

# What about protocols used in real life ?

## E-passport



→ studied in [Arapinis *et al.*, 10]

An electronic passport is a passport with an **RFID tag** embedded in it.



The **RFID tag** stores:

- the information printed on your passport,
- a JPEG copy of your picture.



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The Basic Access Control (BAC) protocol is a key establishment protocol that has been designed to also ensure **unlinkability**.

## ISO/IEC standard 15408

**Unlinkability** aims to ensure *that a user may make multiple uses of a service or resource without others being able to link these uses together.*

# BAC protocol

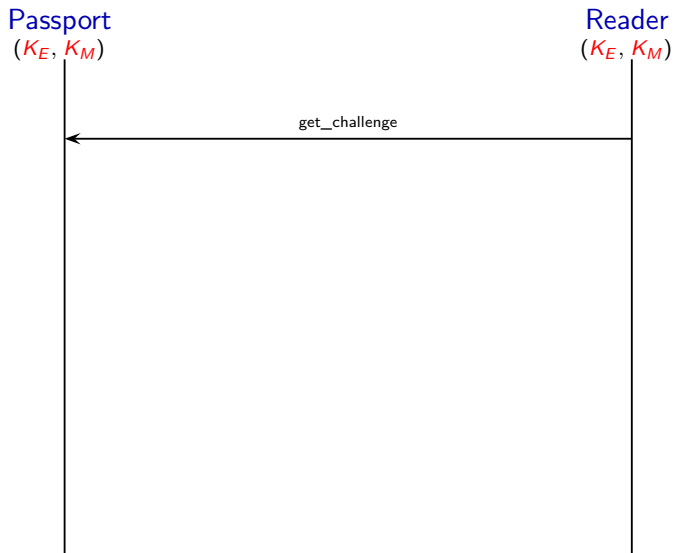
Passport  
 $(K_E, K_M)$



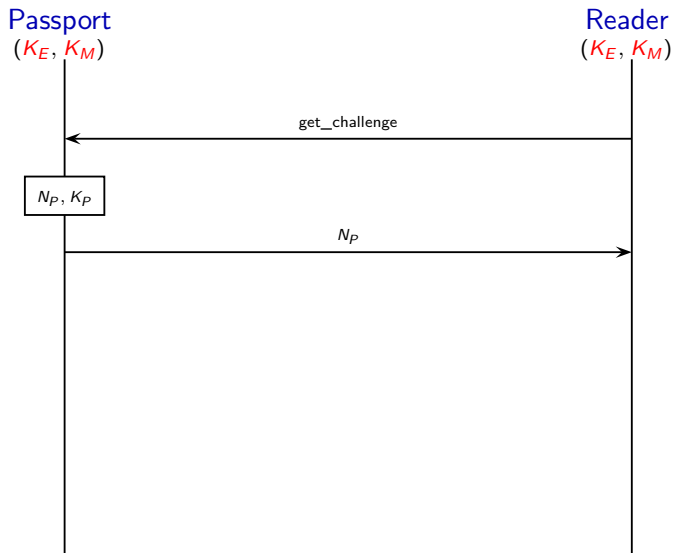
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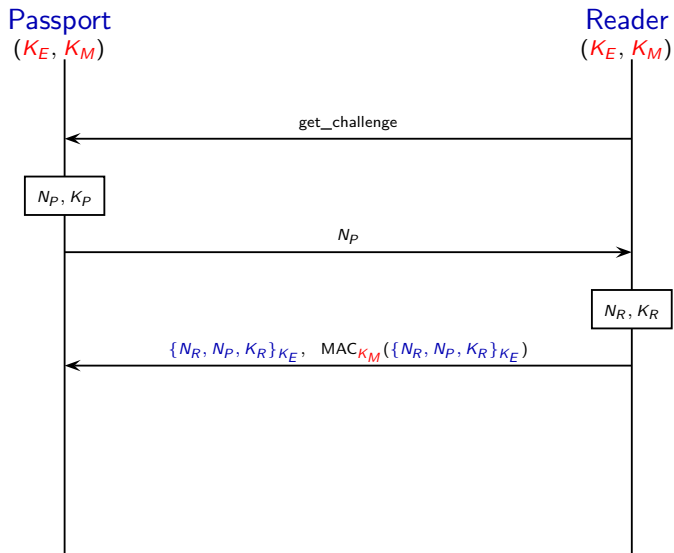
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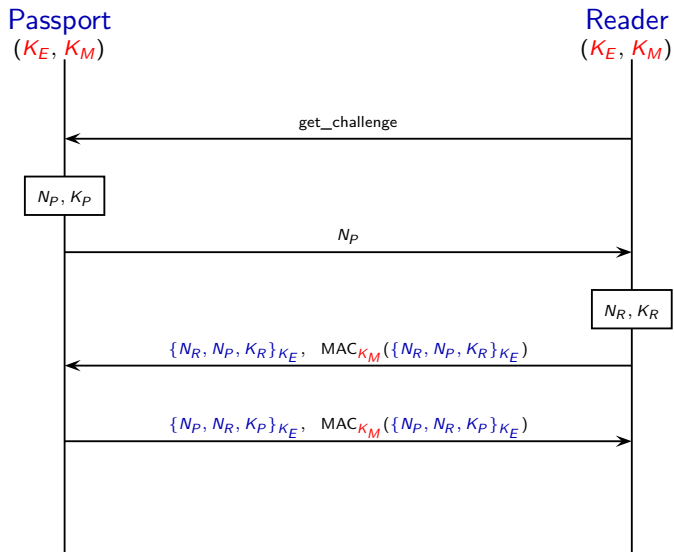
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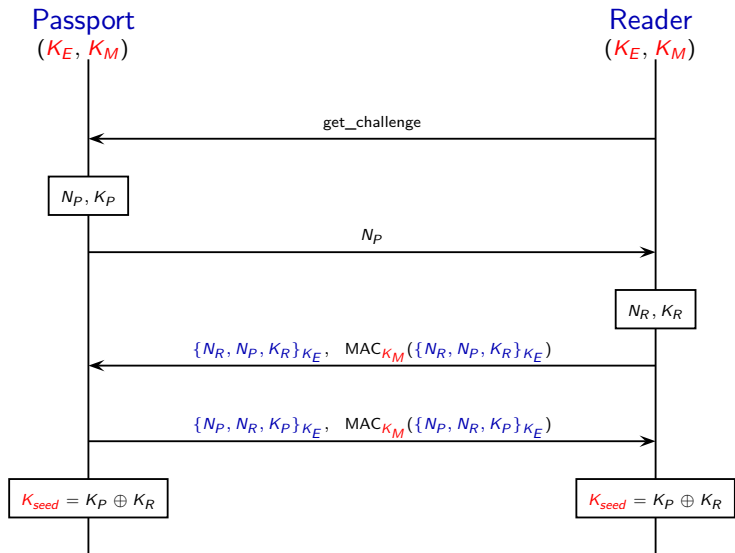
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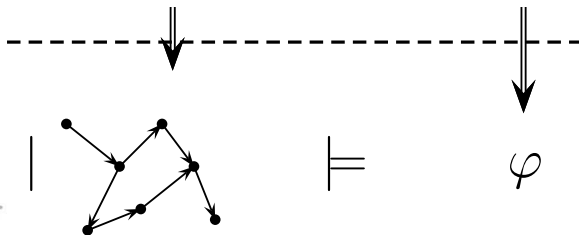
# BAC protocol



# This talk: formal methods for protocol verification

Does the protocol satisfy a security property?

Modelling

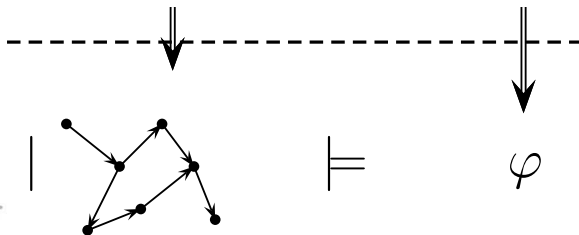




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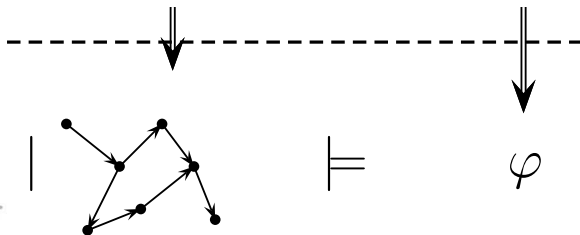
## E-passport application

What about unlinkability of the ePassport holders ?

# This talk: formal methods for protocol verification

Does the **protocol** *satisfy* a **security property**?

Modelling



## Outline of the this talk

- 1 Modelling cryptographic protocols and their security properties
- 2 Designing verification algorithms

## Modelling cryptographic protocols and their security properties

Terms built over a **signature**  $\mathcal{F}$ , and an infinite set of **names**  $\mathcal{N}$ .

$$\begin{array}{l} t ::= \\ \quad | \quad n \quad \text{name } n \\ \quad | \quad f(t_1, \dots, t_k) \quad \text{application of symbol } f \in \mathcal{F} \end{array}$$

Example:

- $\mathcal{F} = \{\text{senc}(\cdot, \cdot), \text{sdec}(\cdot, \cdot), \langle \cdot, \cdot \rangle, \text{proj}_1(\cdot), \text{proj}_2(\cdot)\}$ ;
- $\mathcal{N} = \{n, a, k, s, \dots\}$ .

→ some terms:  $\text{senc}(\langle s, a \rangle, k)$ ,  $\text{sdec}(\text{enc}(s, k), k)$ , and  $s$ .

# Messages as terms

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Term algebra is equipped with an **equational theory**  $E$ .

**Example:**  $\text{dec}(\text{enc}(x, y), y) = x$ ,  $\text{proj}_1(\langle x, y \rangle) = x$ ,  $\text{proj}_2(\langle x, y \rangle) = y$ .

We have that  $\text{sdec}(\text{senc}(s, k), k) =_E s$ .

## Going back to the Denning Sacco protocol

$A \rightarrow B$  :  $\text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B))$

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What function symbols and equations do we need to model this protocol?

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② asymmetric encryption:  $\text{aenc}(\cdot, \cdot)$ ,  $\text{adec}(\cdot, \cdot)$ ,  $\text{pk}(\cdot)$

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③ signature:  $\text{sign}(\cdot, \cdot)$ ,  $\text{check}(\cdot, \cdot)$

$$\longrightarrow \text{check}(\text{sign}(x, y), \text{pk}(y)) = x$$

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- 3 signature:  $\text{sign}(\cdot, \cdot)$ ,  $\text{check}(\cdot, \cdot)$   
 $\longrightarrow \text{check}(\text{sign}(x, y), \text{pk}(y)) = x$

The two terms involved in a normal execution are:

$$\text{aenc}(\text{sign}(k, \text{ska}), \text{pk}(\text{skb})), \text{ and } \text{senc}(s, k)$$

## Applied pi calculus

[Abadi & Fournet, 01]

basic programming language with constructs for **concurrency** and **communication**

→ based on the  $\pi$ -calculus [Milner *et al.*, 92], and in some ways similar to the spi-calculus [Abadi & Gordon, 98]

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### Some advantages:

- allows us to model **cryptographic primitives**
- both **reachability** and **equivalence**-based specification of properties
- **powerful proof techniques** for hand proofs
- some **tool support**, e.g. ProVerif (2001) [Blanchet]  
→ <http://proverif.rocq.inria.fr/>

# Protocols as processes - syntax and semantics

Syntax :	$P, Q$	$:=$	$0$	null process
			$\text{in}(c, x).P$	input
			$\text{out}(c, u).P$	output
			$\text{if } u = v \text{ then } P \text{ else } Q$	conditional
			$P \mid Q$	parallel composition
			$!P$	replication
			$\text{new } n.P$	fresh name generation

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Semantics  $\rightarrow$ :

COMM	$\text{out}(c, M).P \mid \text{in}(c, x).Q \rightarrow P \mid Q\{M/x\}$
THEN	$\text{if } M = N \text{ then } P \text{ else } Q \rightarrow P \text{ when } M =_E N$
ELSE	$\text{if } M = N \text{ then } P \text{ else } Q \rightarrow Q \text{ when } M \neq_E N$

closed by **structural equivalence** ( $\equiv$ ) and application of **evaluation contexts**.

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Alice and Bob as processes:

$P_A(sk_a, pk_b) = \text{new } k. \text{out}(c, \text{aenc}(\text{sign}(k, sk_a), pk_b)).$   
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One possible scenario:

$P_{DS} = \text{new } sk_a, sk_b. (P_A(sk_a, pk(sk_b)) \mid P_B(sk_b, pk(sk_a)))$

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→ this simply models a **normal execution** between two **honest** participants

Confidentiality for process  $P$  w.r.t. secret  $s$

For **all processes**  $A$  such that  $A \mid P \rightarrow^* Q$ , we have that  $Q$  is not of the form  $C[\text{out}(c, s).Q']$  with  $c$  public.

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### Some difficulties:

- we have to consider **all** the possible executions in presence of an **arbitrary adversary** (modelled as a process)
- we have to consider **realistic** initial configurations
  - replications to model an **unbounded** number of sessions,
  - reveal public keys and private keys to model **dishonest** agents,
  - $P_A/P_B$  may play with other (and perhaps) dishonest agents, ...

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## The aforementioned attack

1.  $A \rightarrow C : \text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(C))$

2.  $C(A) \rightarrow B : \text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B))$

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The “minimal” initial configuration to retrieve the attack is:

$\text{new } sk_a. \text{new } sk_b. (P_A(sk_a, \text{pk}(sk_c)) \mid P_B(sk_b, \text{pk}(sk_a)))$



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**Exercise:** Exhibit the process  $A$  (the behaviour of the attacker) that witnesses the aforementioned attack.

## Security properties - privacy

Privacy-type properties are modelled as equivalence-based properties

testing equivalence between  $P$  and  $Q$ ,  $P \approx Q$

for all processes  $A$ , we have that:

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Example 1:

$$\text{out}(a, s) \not\approx \text{out}(a, s')$$

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Example 2:

$$\begin{aligned} & \text{new } s.\text{out}(a, \text{senc}(s, k)).\text{out}(a, \text{senc}(s, k')) \\ & \quad \neq \\ & \text{new } s, s'.\text{out}(a, \text{senc}(s, k)).\text{out}(a, \text{senc}(s', k')) \end{aligned}$$

$\longrightarrow A = \text{in}(a, x).\text{in}(a, y).\text{if } (\text{sdec}(x, k) = \text{sdec}(y, k')) \text{ then out}(c, \text{ok})$

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**Exercise:** Are the two following processes in testing equivalence?

$$\text{new } s.\text{out}(a, s) \stackrel{?}{\approx} \text{new } s.\text{new } k.\text{out}(a, \text{enc}(s, k))$$

# Going back to the e-passport protocol

## What does unlinkability mean?

**Informally**, an observer can not observe the difference between the two following situations:

- 1 a situation where the same passport may be used **twice** (or even more);
- 2 a situation where each passport is used **at most once**.





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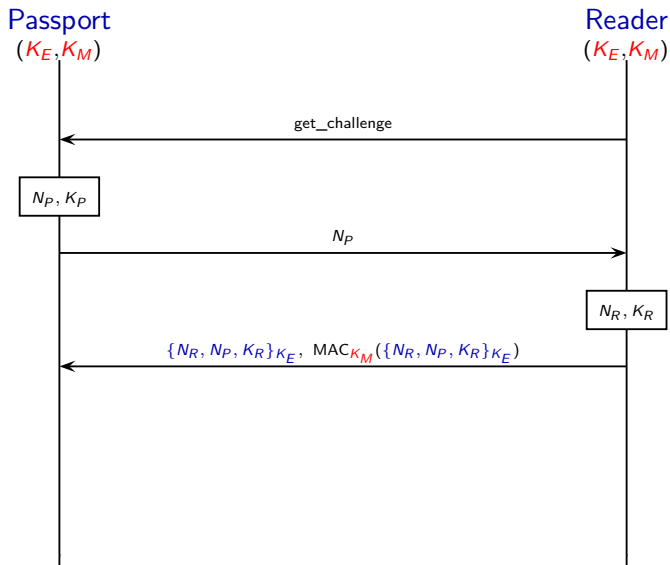


More precisely, we have that:

$$\begin{aligned} & !\text{new } ke.\text{new } km.(!P_{\text{Pass}} \mid !P_{\text{Reader}}) \\ & \quad ? \\ & \quad \approx \\ & !\text{new } ke.\text{new } km.( P_{\text{Pass}} \mid !P_{\text{Reader}}) \end{aligned}$$

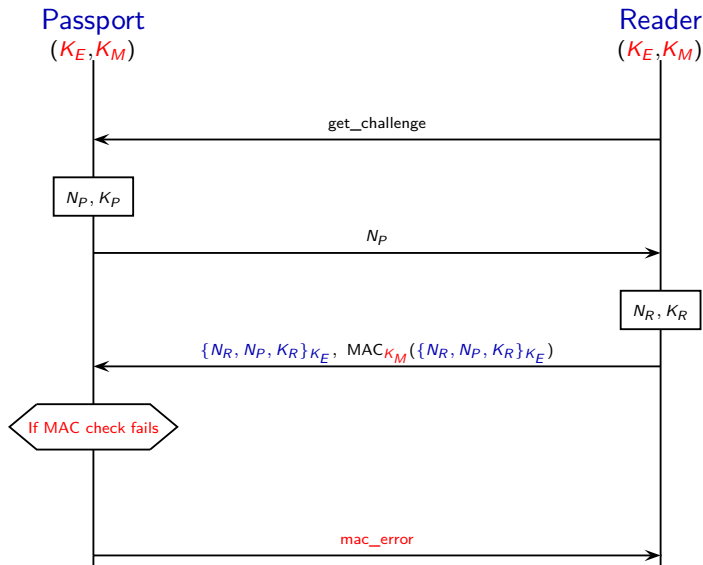
# French electronic passport

→ the passport must reply to all received messages.



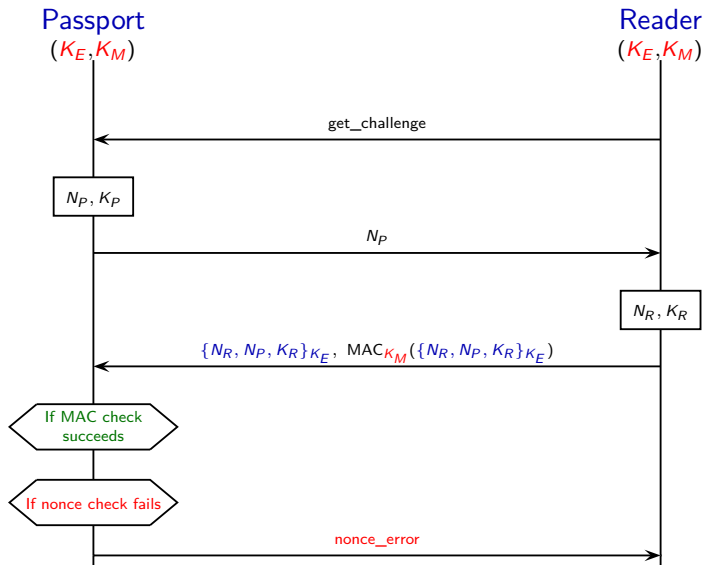
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# An attack on the French passport

## Attack against unlinkability

[Chothia & Smirnov, 10]

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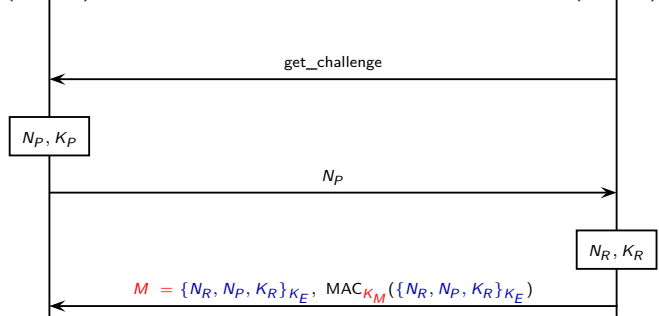
**Part 1 of the attack.** The attacker eavesdrops on Alice using her passport and records message  $M$ .

Alice's Passport

$(K_E, K_M)$

Reader

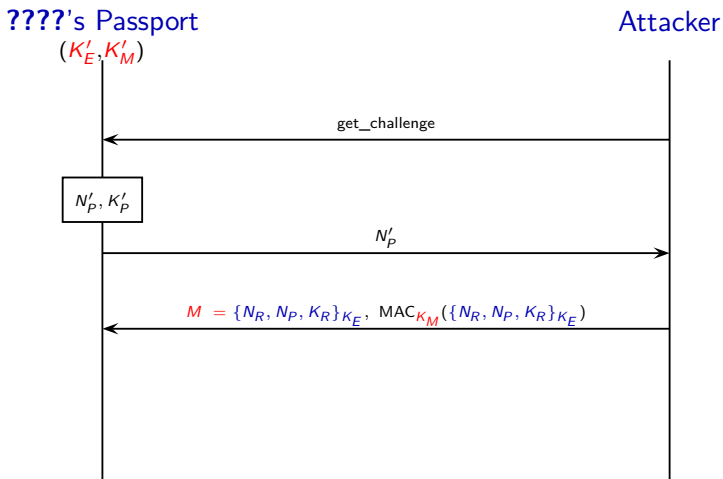
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# An attack on the French passport

## Part 2 of the attack.

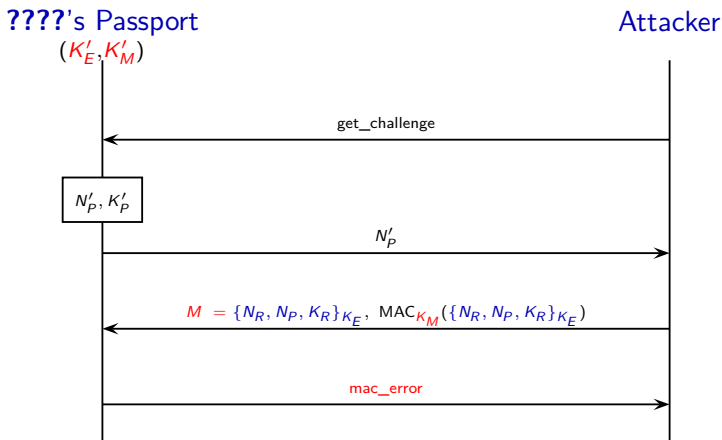
The attacker replays the message  $M$  and checks the error code he receives.



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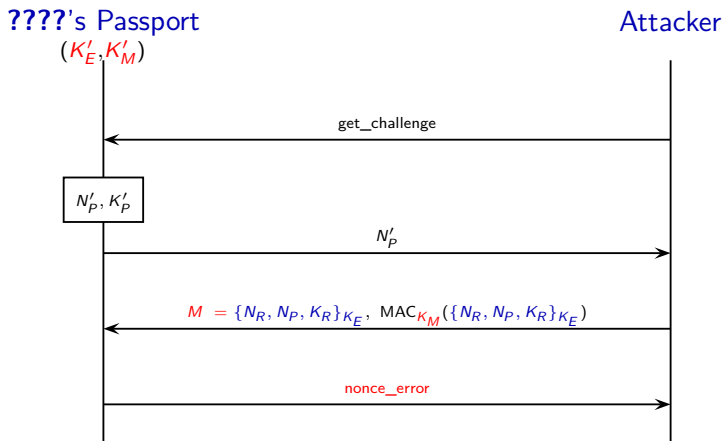
$\implies$  MAC check failed  $\implies K'_M \neq K_M \implies$  **???? is not Alice**



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The attacker replays the message  $M$  and checks the error code he receives.



$\implies$  MAC check succeeded  $\implies K'_M = K_M \implies$  **???? is Alice**

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## Attack !

The equivalence does not hold:  $P_{\text{same}} \not\approx P_{\text{diff}}$ .



More formally,

$$P_{\text{same}} \stackrel{\text{def}}{=} !\text{new } ke.\text{new } km.(!P_{\text{Pass}} \mid !P_{\text{Reader}})$$
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**Exercise:** Exhibit the process  $A$  that witnesses the attack.

## Designing verification algorithms

### ① From confidentiality ...

→ *i.e.* trace-based security properties

### ② ... to privacy

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# State of the art in a nutshell

for analysing trace-based security properties

Unbounded number of sessions

- **undecidable** in general [Even & Goldreich, 83; Durgin *et al*, 99]

→ **ProVerif**: A tool that does not correspond to any decidability result but works well in practice. [Blanchet, 01]

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## Bounded number of sessions

- a **decidability** result (NP-complete) [Rusinowitch & Turuani, 01; Millen & Shmatikov, 01]

- result extended to deal with various cryptographic primitives.

→ various automatic tools, e.g. **AVISPA platform** [Armando *et al.*, 05]

▶ Skip

# The deduction problem: is $u$ deducible from $T$ ?

We consider a **signature**  $\mathcal{F}$  and an **equational theory**  $E$ .

## The deduction problem

**input** A sequence  $\phi$  of ground terms (*i.e.* messages) and a term  $s$  (the secret)  
$$\phi = \{w_1 \triangleright v_1, \dots, w_n \triangleright v_n\}$$

**output** Can the attacker learn  $s$  from  $\phi$ , *i.e.* does there exist a term (called **recipe**)  $R$  built using public symbols and  $w_1, \dots, w_n$  such that  $R\phi =_E s$ .



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**Example:** Let  $\phi = \{w_1 \triangleright \text{pk}(ska); w_2 \triangleright \text{pk}(skb); w_3 \triangleright \text{skc}; w_4 \triangleright \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)); w_5 \triangleright \text{senc}(s, k)\}$ .

We have that:

- $k$  is deducible from  $\phi$  using  $R_1 = \text{check}(\text{adec}(w_4, w_3), w_1)$ ,
- $s$  is deducible from  $\phi$  using  $R_2 = \text{sdec}(w_5, R_1)$ .

## Proposition

The **deduction problem** is decidable in PTIME for the equational theory modelling the DS protocol (and for many others)

Proof (sketch)

- 1 saturation of  $\phi$  with its deducible subterm  $\phi^+$
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→ The deduction problem is actually decidable for many interesting equational theories.

# Confidentiality using the constraint solving approach

→ for a bounded number of sessions

Two main steps:

- 1 A **symbolic** exploration of all the possible traces  
The infinite number of possible traces (*i.e.* experiment) are represented by a finite set of constraint systems  
→ this set can be huge (exponential on the number of sessions) ...  
but some optimizations are used to reduce this number
- 2 A decision procedure for deciding whether a constraint system has a solution or not.  
→ this algorithm works quite well

# Confidentiality via constraint solving

Constraint systems are used to specify confidentiality (or more generally any trace-based property) under a particular scenario.

## Protocol rules

- a particular interleaving -

in( $u_1$ );

out( $v_1$ ); in( $u_2$ );

...

out( $v_n$ )

## Constraint System

$$\mathcal{C} = \left\{ \begin{array}{l} T_0 \stackrel{?}{\vdash} u_1 \\ T_0, v_1 \stackrel{?}{\vdash} u_2 \\ \dots \\ T_0, v_1, \dots, v_n \stackrel{?}{\vdash} s \end{array} \right.$$

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## Solution of a constraint system $\mathcal{C}$

A substitution  $\sigma$  such that

for every  $T \stackrel{?}{\vdash} u \in \mathcal{C}$ ,  $u\sigma$  is deducible from  $T\sigma$ .

for every  $u = v \in \mathcal{C}$  (resp.  $u \neq v$ ),  $u\sigma =_E v\sigma$  (resp.  $u\sigma \neq_E v\sigma$ )

# Going back to the Denning Sacco protocol

$A \rightarrow B$  :  $\text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B))$

$B \rightarrow A$  :  $\text{senc}(s, k)$

One possible interleaving:

$\text{out}(\text{aenc}(\text{sign}(k, ska), pk(skb)))$

$\text{in}(\text{aenc}(\text{sign}(x, ska), pk(skb))); \text{out}(\text{senc}(s, x))$



# Going back to the Denning Sacco protocol

$$\begin{aligned} A \rightarrow B & : \text{aenc}(\text{sign}(k, \text{priv}(A)), \text{pub}(B)) \\ B \rightarrow A & : \text{senc}(s, k) \end{aligned}$$

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**Question:** Does  $\mathcal{C}$  admit a solution?    **Yes:**  $x \rightarrow k$ .

# The general case: is the constraint system $\mathcal{C}$ satisfiable?

Main idea: simplify them until reaching  $\perp$  or solved forms

Constraint system in solved form

$$\mathcal{C} = \left\{ \begin{array}{l} T_0 \stackrel{?}{\vdash} x_0 \\ T_0 \cup T_1 \stackrel{?}{\vdash} x_1 \\ \dots \\ T_0 \cup T_1 \dots \cup T_n \stackrel{?}{\vdash} x_n \end{array} \right.$$

## Question

Is there a solution to such a system ?

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## Question

Is there a solution to such a system ?

Of course, yes ! Choose  $u_0 \in T_0$ , and consider the substitution:

$$\sigma = \{x_0 \mapsto u_0, \dots, x_n \mapsto u_0\}$$

# Simplification rules

→ these rules deal with pairs and symmetric encryption only

$$R_{\text{ax}} : \mathcal{C} \wedge T \vdash^? u \rightsquigarrow \mathcal{C} \quad \text{if } T \cup \{x \mid T' \vdash^? x \in \mathcal{C}, T' \subsetneq T\} \vdash u$$

$$R_{\text{unif}} : \mathcal{C} \wedge T \vdash^? u \rightsquigarrow_{\sigma} \mathcal{C}\sigma \wedge T\sigma \vdash^? u\sigma \\ \text{if } \sigma = \text{mgu}(t_1, t_2) \text{ where } t_1, t_2 \in \text{st}(T) \cup \{u\}$$

$$R_{\text{fail}} : \mathcal{C} \wedge T \vdash^? u \rightsquigarrow \perp \quad \text{if } \text{vars}(T \cup \{u\}) = \emptyset \text{ and } T \not\vdash u$$

$$R_f : \mathcal{C} \wedge T \vdash^? f(u_1, u_2) \rightsquigarrow \mathcal{C} \wedge T \vdash^? u_1 \wedge T \vdash^? u_2 \quad f \in \{\langle \rangle, \text{senc}\}$$

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**Example:**  $T_0; \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)) \vdash^? \text{aenc}(\text{sign}(x, ska), \text{pk}(skb))$

$$\rightsquigarrow \text{(with } R_f) \left\{ \begin{array}{l} T_0; \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)) \vdash^? \text{sign}(x, ska) \\ T_0; \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)) \vdash^? \text{pk}(skb) \end{array} \right.$$

# Exercise - still about the Denning Sacco protocol

## Exercise

Reach a solved form starting with the constraint system:

$$\begin{array}{l} T_0; \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)) \quad \vdash^? \quad \text{aenc}(\text{sign}(x, ska), \text{pk}(skb)) \\ T_0; \text{aenc}(\text{sign}(k, ska), \text{pk}(skc)); \text{senc}(s, x) \quad \vdash^? \quad s \end{array}$$

You should be able to reach a constraint system in **solved form** (actually the empty one) in 3 steps.

**Hint:**  $R_{\text{ax}}$  and  $R_{\text{unif}}$  twice.



# Results on the simplification rules

Given a (well-formed) constraint system  $\mathcal{C}$ :

**Soundness:**

If  $\mathcal{C} \rightsquigarrow_{\sigma}^* \mathcal{C}'$  and  $\theta$  solution of  $\mathcal{C}'$  then  $\sigma\theta$  is a solution of  $\mathcal{C}$ .

→ easy to show

**Completeness:**

If  $\theta$  is a solution of  $\mathcal{C}$  then there exists  $\mathcal{C}'$  and  $\theta'$  such that  $\mathcal{C} \rightsquigarrow_{\sigma}^* \mathcal{C}'$ ,  $\theta'$  is a solution of  $\mathcal{C}'$ , and  $\theta = \sigma\theta'$ .

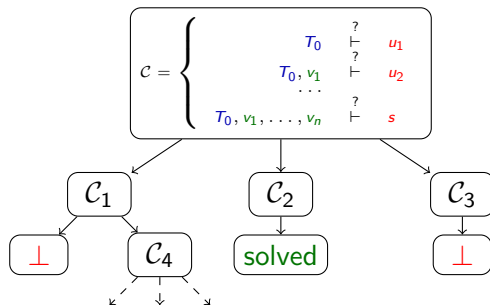
→ more involved to show

**Termination:** There is no infinite chain  $\mathcal{C} \rightsquigarrow_{\sigma_1} \mathcal{C}_1 \dots \rightsquigarrow_{\sigma_n} \mathcal{C}_n$ .

→ using the lexicographic order (number of var, size of rhs)

# Procedure for solving a constraint system

Main idea of the procedure:

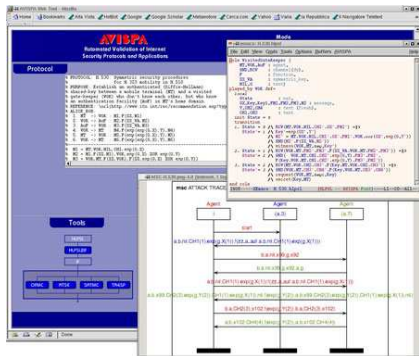


→ this gives us a symbolic **representation** of **all** the solutions.

# Results and tools

## Theorem

Deciding confidentiality for a **bounded number of sessions** is **decidable** for classical primitives (actually in co-NP).



→ This approach has been implemented in the AVISPA Platform  
<http://www.avispa-project.org/>

## Designing verification algorithms

① From confidentiality ...

→ *i.e.* trace-based security properties

② ... **to privacy**

→ ***i.e.* equivalence-based security properties**

# State of the art in a nutshell

for analysing equivalence-based security properties

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for analysing equivalence-based security properties

Unbounded number of sessions

[Blanchet, Abadi & Fournet, 05]

ProVerif tool

<http://www.proverif.ens.fr/>

- + various cryptographic primitives;
  - - termination is not guaranteed; diff-equivalence (**too strong**)
- some extensions to go beyond diff-equivalence

Bounded number of sessions

e.g. [Baudet, 05], [Dawson & Tiu, 10], [Chevalier & Rusinowitch, 10], ...

→ this allows one to decide testing equivalence between “simple” processes without else branch.

**None of these results is able to analyse the e-passport protocol.**

→ V. Cheval, H. Comon-Lundh, and S. Delaune    CCS 2011

## Main result

A procedure for deciding testing equivalence for a large class of processes for a bounded number of sessions.

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A procedure for deciding testing equivalence for a large class of processes for a bounded number of sessions.

## Our class of processes:

- + non-trivial else branches, private channels, and non-deterministic choice;
- – a fixed set of cryptographic primitives (signature, encryption, hash function, mac).

→ this allows us in particular to deal with the e-passport example



# The ground case: are $\phi$ and $\psi$ in static equivalence?

## The static equivalence problem

**input** Two frames  $\phi$  and  $\psi$

$$\phi = \{w_1 \triangleright u_1, \dots, w_\ell \triangleright u_\ell\} \quad \psi = \{w_1 \triangleright v_1, \dots, w_\ell \triangleright v_\ell\}$$

**output** Can the attacker distinguish the two frames, *i.e.* does there exist a **test**  $R_1 \stackrel{?}{=} R_2$  such that:

$$R_1\phi =_E R_2\phi \text{ but } R_1\psi \neq_E R_2\psi \text{ (or the converse).}$$

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**Example:** Consider the frames:

- $\phi = \{w_1 \triangleright \text{aenc}(\langle \text{yes}, r_1 \rangle, \text{pk}(sks)); w_2 \triangleright sks\}$ ; and
- $\psi = \{w_1 \triangleright \text{aenc}(\langle \text{no}, r_2 \rangle, \text{pk}(sks)); w_2 \triangleright sks\}$ .

They are **not** in static equivalence:  $\text{proj}_1(\text{adec}(w_1, w_2)) \stackrel{?}{=} \text{yes}$ .

# The ground case

## Proposition

The **static equivalence problem** is decidable in PTIME for the theory modelling the DS protocol (and for many others)

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Proof (sketch)

- 1 saturation of  $\phi/\psi$  with their deducible subterms  $\phi^+/\psi^+$
- 2 does there exist a test  $R_1 \stackrel{?}{=} R_2$  such that  $R_1\phi^+ = R_2\phi^+$  whereas  $R_1\psi^+ \neq R_2\psi^+$  (again syntactic equality) ?  
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## Going back to the previous example:

- $\phi^+ = \phi \uplus \{w_3 \triangleright \langle \text{yes}, r_1 \rangle; w_4 \triangleright \text{yes}; w_5 \triangleright r_1\}$ , and
- $\psi^+ = \psi \uplus \{w_3 \triangleright \langle \text{no}, r_2 \rangle; w_4 \triangleright \text{no}; w_5 \triangleright r_2\}$ .

→  $\phi^+$  and  $\psi^+$  are **not** in static equivalence:  $w_4 \stackrel{?}{=} \text{yes}$ .

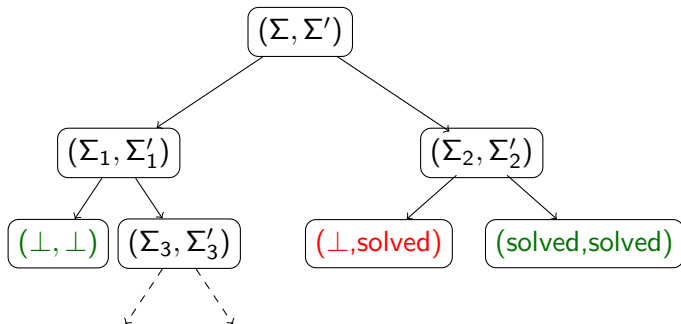
# Privacy using the constraint solving approach

Two main steps:

- 1 A **symbolic** exploration of all the possible traces  
The infinite number of possible traces (*i.e.* experiment) are represented by a finite set of constraint systems  
→ this set can be huge (exponential on the number of sessions) !
- 2 A decision procedure for deciding (symbolic) **equivalence between sets of constraint systems**  
→ this algorithm works quite well

# Deciding symbolic equivalence

**Main idea:** We rewrite pairs  $(\Sigma, \Sigma')$  of sets of constraint systems (extended to keep track of some information) until a trivial failure or a trivial success is found.



# Results on the simplification rules

## Termination

Applying blindly the simplification rules does not terminate but there is a particular **strategy**  $\mathcal{S}$  that allows us to ensure termination.

## Soundness/Completeness

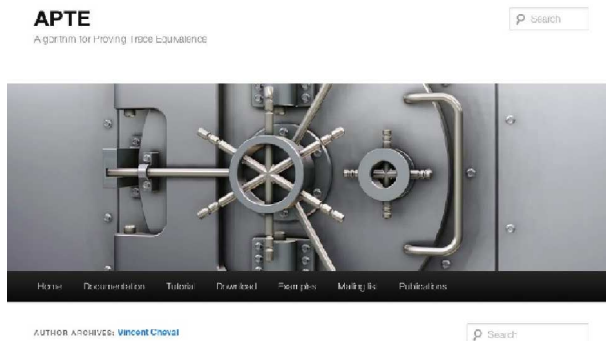
Let  $(\Sigma_0, \Sigma'_0)$  be pair of sets of constraint systems, and consider a binary tree obtained by applying our simplification rule following a strategy  $\mathcal{S}$ .

- 1 **soundness**: If all leaves of the tree are labeled with  $(\perp, \perp)$  or  $(solved, solved)$ , then  $\Sigma_0 \approx_s \Sigma'_0$ .
- 2 **completeness**: if  $\Sigma_0 \approx_s \Sigma'_0$ , then all leaves of the tree are labeled with  $(\perp, \perp)$  or  $(solved, solved)$ .



## Theorem

Deciding testing equivalence between processes **without replication** for classical primitives is **decidable**.



→ This approach has been implemented in APTE by Vincent CHEVAL

<http://projects.lsv.ens-cachan.fr/APTE>

# Limitations of these approaches

- 1 the algebraic properties of the primitives are **abstracted away**  
→ no guarantee if the protocol relies on an encryption that satisfies some additional properties (e.g. RSA, ElGamal)
- 2 only the specification is analysed and **not the implementation**  
→ most of the passports are actually linkable by a careful analysis of time or message length.

<http://www.loria.fr/~glondu/epassport/attaque-tailles.html>

- 3 not all scenarios are checked  
→ no guarantee if the protocol is used **one more time** !

## **A need of formal methods in verification of security protocols.**

Regarding confidentiality (or authentication), powerful tool support that are nowadays used by industrials and security agencies.

**It remains a lot to do for analysing privacy-type properties:**

- formal definitions of some subtle security properties
- algorithms (and tools!) for checking automatically trace equivalence for various cryptographic primitives;
- more composition results.

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### VIP - Verification of Indistinguishability Properties

Main topics of the ANR JCJC - VIP project  
(Jan. 2012 - Dec 2015)

<http://www.lsv.ens-cachan.fr/Projects/anr-vip/>

→ **A post-doc position (for 1 year) is available on this project.**